



# Few Shot Learning

Machine Learning that scales

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# INTRODUCTION

General Overview

Examples

Basic Principles

# Problems

- Amount of labeled data
- Retraining for new examples
- Classes unavailable during training
- Large number of classes

## Big Dataset Absurd

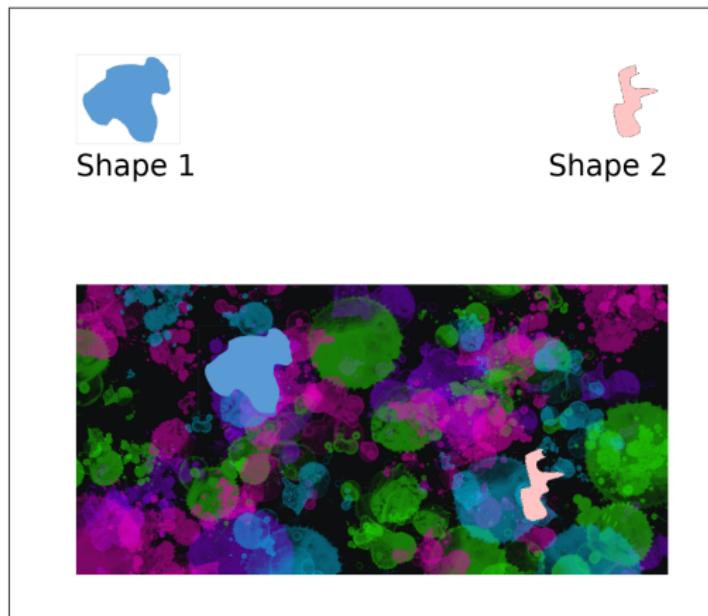


Figure: Shape recognition absurd

# Person Re-Identification



Figure: Viewing the same scene with two cameras

# Wake-up Word Detection



Figure: Learning Acoustic Word Embeddings [HYYH18]

# Definition

***One-shot learning*** is an object categorization problem which aims to learn information about object categories from one, or only a few, training samples.

# Historical View

- Instance based algorithms (KNN)
- Mahalanobis distance [Mah36]
- Metrics learning
- Siamese neural networks [BGL<sup>+</sup>93]

# K - Nearest Neighbours

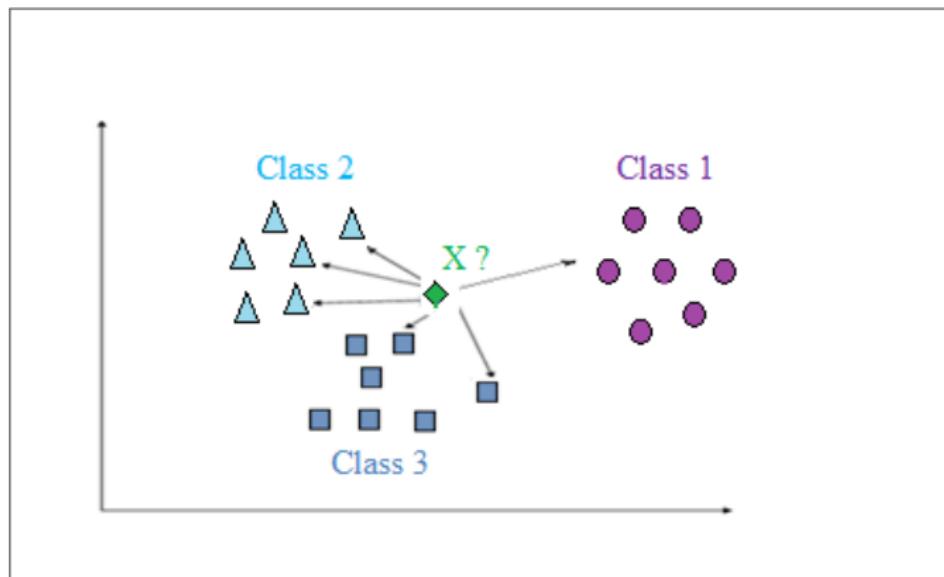


Figure: K - Nearest Neighbours

# Mahalanobis Distance

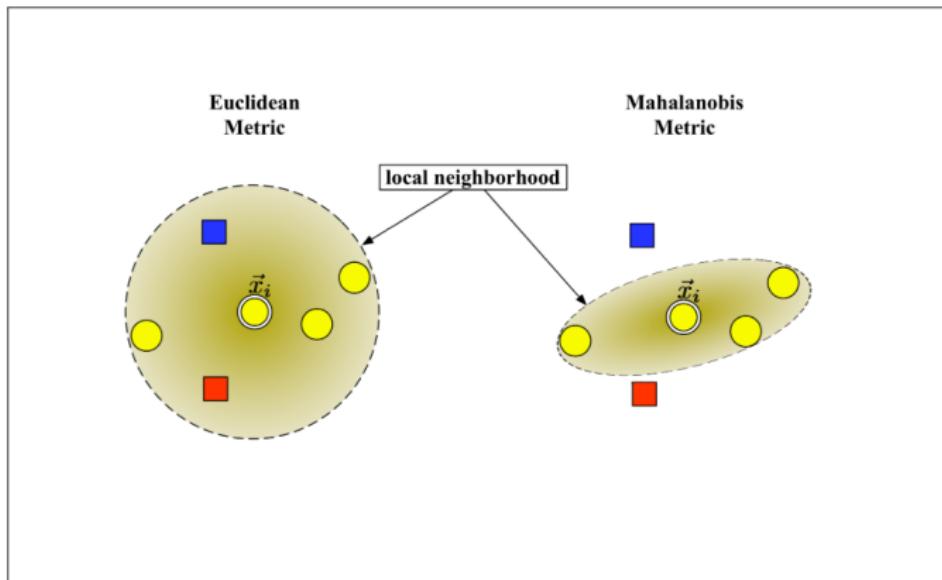


Figure: Local Neighbourhoods

# Mahalanobis Distance - Formulation

## Definition

Let  $x, y \in \mathcal{D} \subseteq \mathbb{R}^n$  with the covariance matrix  $\Sigma$ . Mahalanobis distance  $d : \mathbb{R}^n \times \mathbb{R}^n \rightarrow \mathbb{R}$  is defined as follows:

$$d(x, y) = \sqrt{(x - y)^T \Sigma^{-1} (x - y)}$$

# Mahalanobis Distance - Properties

- Performs better
- Invariant to linear transformations
- Fast to compute
- Assumes linear correlation

# Nonlinearity

*We're living in a **non-linear** world!*

*Madonna*

# Embeddings

- Transform data in a non-linear manner
- Maintain semantic information
- Learn distance function <sup>1</sup>
- Measure distance on embedded objects

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<sup>1</sup>or enforce embedding to be a euclidian space.

# Siamese Architecture

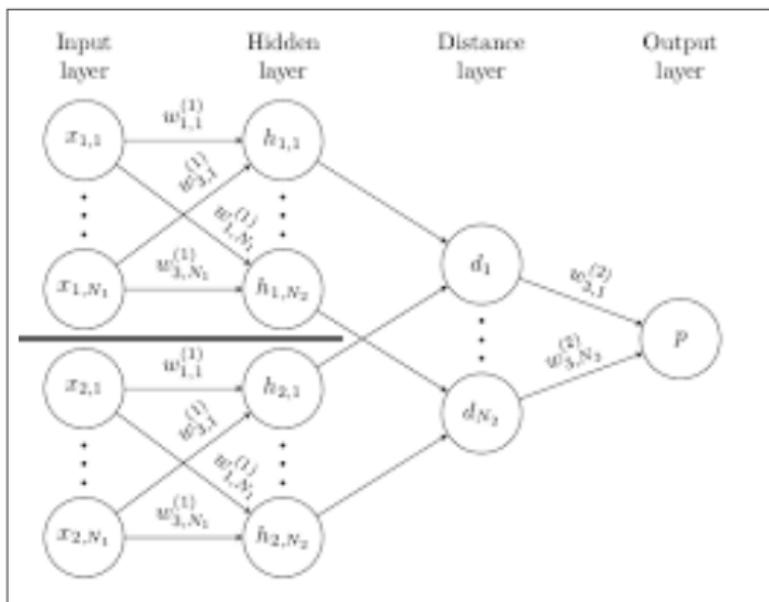


Figure: Siamese Neural Networks [GK15]

# STANDARD TECHNIQUES

Contrastive Loss

Triplet Loss

Quadruplet Loss

Matching Networks

More of Influential Papers

# Metric Learning

- Probabilistic models vs. Energy-based models [LJH05]
- Low-dimensional embedding:  $G_W(X)$
- Similarity metric:  $E_W(X_1, X_2) = \|G_W(X_1) - G_W(X_2)\|$  [CHL05]

# Siamese EBM

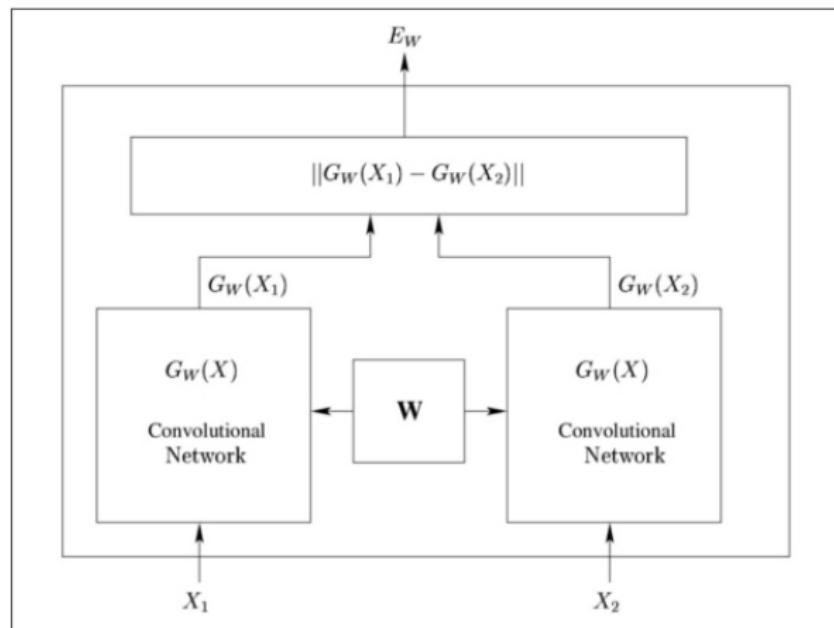


Figure: EBM model with siamese architecture

# Contrastive Loss

$$\blacksquare \quad \mathcal{L}(W) = \sum_{i=1}^n L(W, (Y, X_1, X_2)^i)$$

# Contrastive Loss

- $\mathcal{L}(W) = \sum_{i=1}^n L(W, (Y, X_1, X_2)^i)$
- $L(W, (Y, X_1, X_2)^i) = (1 - Y)L_G(E_W(X_1, X_2)^i) + (Y)L_I(E_W(X_1, X_2)^i)$

# Contrastive Loss

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- $L_G(E_W(X_1, X_2)) = \frac{2}{Q}(E_W(X_1, X_2))^2$
- $L_I(E_W(X_1, X_2)) = 2Qe^{-\frac{2.77}{Q}E_W(X_1, X_2)}$

# Triplet Loss - Setup

Unified embedding for Face Recognition and Clustering  
[SKP15]

- Provide embedding
- Euclidian space
- Triplets: anchor, positive, and negative

# Triplet Loss - Disclaimer

*Although we did not directly compare to other losses,  
we believe that the triplet loss is more suitable for face  
verification.*

# Triplet Loss - Visualization

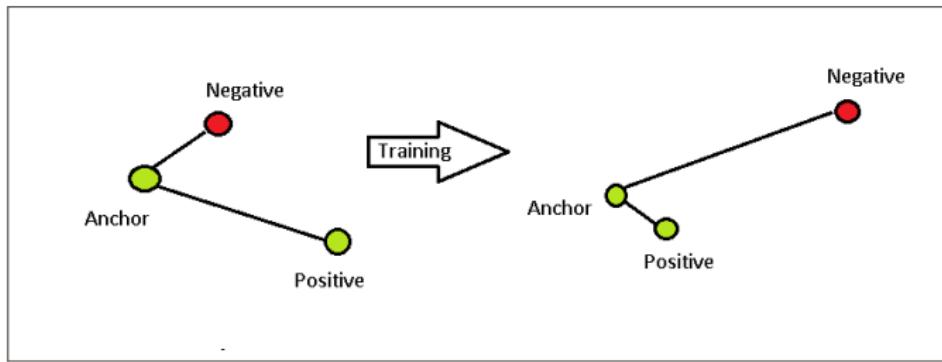


Figure: Triplet loss - training objective

# Triplet Loss - Formulation

For  $i$ -th triplet  $(x_i^a, x_i^p, x_i^n) \in \mathcal{T}$  and embedding function  $f_W$ :

$$\left\| f_W(x_i^a) - f_W(x_i^p) \right\|_2^2 + \alpha < \left\| f_W(x_i^a) - f_W(x_i^n) \right\|_2^2$$

# Triplet Loss - Formulation

For  $i$ -th triplet  $(x_i^a, x_i^p, x_i^n) \in \mathcal{T}$  and embedding function  $f_W$ :

$$\mathcal{L}(W) = \sum_i^{|\mathcal{T}|} \left\| f_W(x_i^a) - f_W(x_i^p) \right\|_2^2 - \left\| f_W(x_i^a) - f_W(x_i^n) \right\|_2^2 + \alpha$$

# Triplet Mining

For given example  $x_i^a$ , the following instances are important:

- Hard positive:  $x_i^{hp} = \operatorname{argmax}_{x_i^p} \|f_W(x_i^a) - f_W(x_i^p)\|_2^2$
- Hard negative:  $x_i^{hn} = \operatorname{argmin}_{x_i^n} \|f_W(x_i^a) - f_W(x_i^n)\|_2^2$

# Triplet Mining

- Online mini-batch mining
- Fix the number of anchors per mini-batch (40)
- Include all positive examples in mini-batch
- Sample additional negative examples
- Use semi-hard negative examples (local minima)

# Quadruplet Loss - Introduction

Beyond triplet loss: a deep quadruplet network for person re-identification [CCZH17]

- Triplets has low generalization
- QL gives smaller intra-class variation
- QL gives bigger inter-class variation
- Learn metric  $g(x_i, x_j)$  instead of euclidian distance

# QL - Embeddings

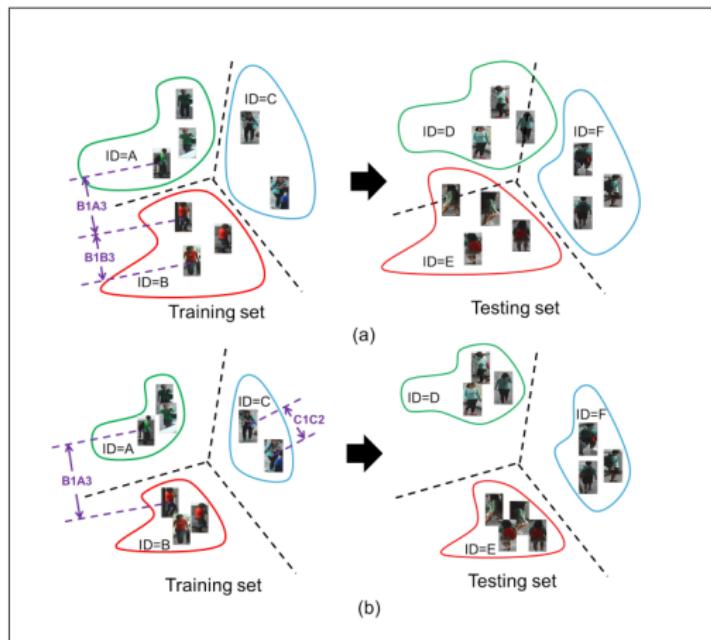


Figure: Embeddings with triplet loss (a) vs. QL (b)

# QL - Formulation

- Modified triplet loss:

$$L_{trp} = \sum_{i,j,k}^N [g(x_i, x_j)^2 - g(x_i, x_k)^2 + \alpha_{trp}]_+$$

- Quadruplet loss:

$$L_{quad} = L_{trp} + \sum_{i,j,k,l}^N [g(x_i, x_j)^2 - g(x_l, x_k)^2 + \alpha_2]_+$$

# Matching Networks - Introduction

- Using a support set:  $S$
- Learn mapping:  $S \rightarrow c(\hat{x})$
- Use attention mechanism over support set
- $\hat{y} = \operatorname{argmax}_y P(y|\hat{x}, S)$

# Matching Networks - Visualization

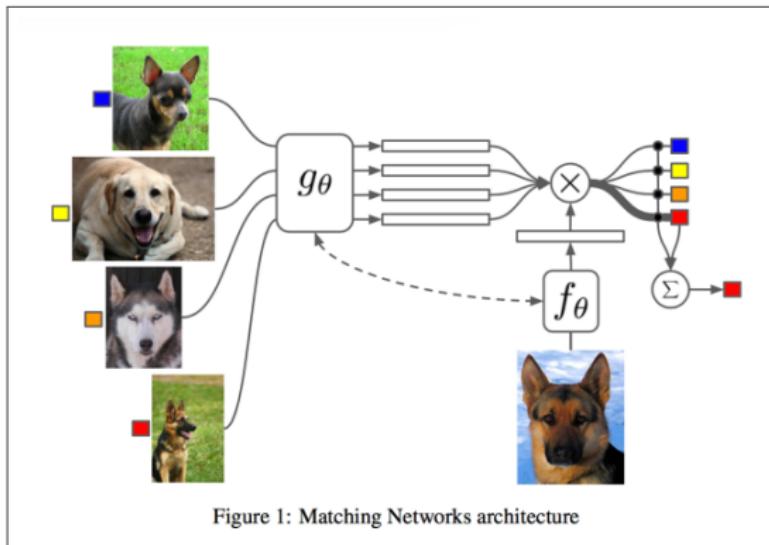


Figure: Matching Network Architecture

# Matching Networks - Formulation

- $\hat{y} = \sum_{i=1}^k a(\hat{x}, x_i) y_i$
- $a(\hat{x}, x_i) = \frac{e^{c(f(\hat{x}), g(x_i))}}{\sum_{j=1}^k e^{c(f(\hat{x}), g(x_j))}}$

# Matching Networks - Training

- Task T - distribution over possible labels L
- Sample L from T
- Use L to sample S and B from the dataset
- Minimise error in batch B, given S

$$\theta = \operatorname{argmax}_{\theta} E_{L \sim T}[E_{S \sim L, B \sim L} \left[ \sum_{(x,y) \in B} \log P_{\theta}(y|x, S) \right]]$$

# More of Influential Papers

- Lifted Structured Feature Embedding [SXJS15]
- Angular Loss [WZW<sup>+</sup>17]
- Cosine Metric Learning [WB18]
- In Defense of the Triplet Loss [HBL17]

FIN

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